

§11.1.

Synopsis: Chapter Eleven.

Briggs establishes three methods of subtabulation in his growing table of logarithms, in this and in the two following chapters. The first method is simple proportion, which he has discovered does not work very well either for tables of logarithms or any others. However, he has found the best region for interpolation to be where the differences between known logarithms are smallest and changing slowest, for equal increases of the absolute numbers: which occurs near the number 100,000. A method based on this fact is used to find a good approximation to the number corresponding to a known logarithm: by moving the logarithm to this part of the table by adding the logarithm of a selected number, interpolating in the 'linear' region to find the approximate composite number, and then returning to the original position on dividing by the selected number.

§11.2.

Chapter Eleven. [p.21.]

To improve on the accuracy of a number found from the Chiliades by the use of a proportional part.

By these methods we have shown how we can find the logarithms of all numbers, prime and composite, whole and fractional. Of these, we have described thirty Chiliads¹, comprised of two columns. The first on the left-hand side of these contains the absolute numbers in the series of natural numbers increasing from 1 to 20,000: then this interrupted series, from 90,000 to 100,000. The other column near the former, has the logarithms of the absolute numbers, and the differences of these: which not only show the errors, if by chance these have crept in; but also provide a proportional part, as often as necessary; in order that we can find a little more accurately that which is had in the table itself. But that proportional part, which is acquired through these differences, is not absolutely perfect; but always departs a little from that absolute accuracy we are looking for. Indeed, since the absolute numbers increase everywhere uniformly, but the logarithms which are greater have smaller increments there: if for an absolute number, the logarithm of the number nearest should be increased by a proportional part, that part sought interposed by the difference, will always be less than it ought to be. But on the other hand, if for a given logarithm the absolute number is sought, that part will be increased more by the proportional part from the regular amount². The same inconvenience happens with sines, tangents, and secants; and entirely with all tables of numbers, where the differences from the one part are equal and unequal for the other. Nevertheless, where the inequality of the differences is small, there the difference from the

true value will be small. For that reason, the proportional part recedes further from the true value in the earlier Chiliads than in the latter; from which we shall be able to produce [an increase in accuracy] in this way. (How often the need arises to investigate a number sought more carefully, and the leisure there might have been [!])

The given logarithm (of which the absolute number is sought), in the first place drops the characteristic, (which does not change the number sought in any way, but only to move it forward by a higher step to a place more removed from unity) then taken away from the logarithm of ten, 1,00000,00000,0000. For the remainder, not inconveniently, will be called the arithmetical complement. This remainder (by adding first the characteristic seen by us to be the most useful) we seek among the Chiliads, and the nearest smaller logarithm selected, and (with the absolute number of the same logarithm reserved at the time) it is added to the given logarithm. The total by necessity falls into the final Chiliad, in which the corresponding absolute number of the same is taken, which through the added proportional part we can correct. This number, found and corrected, is divided by the first number set aside before; the quotient is the number agreeing with the given logarithm, which we sought in the first place. Take this example of this instruction. The mean proportional between unity and 1200 is sought, of which the logarithm is 3,07918,12460,4762. But the logarithm of the mean sought is half of this, by the definition of the logarithm, Ch.1 & 2; Axiom 2,Ch.2, which is of course, 1,53959,06230,2381. Which with the characteristic removed and taken from 1,00000,00000,0000 leaves 0,46040,93769,7619. The nearest logarithm to this, if we ignore the characteristic, is found in the third Chiliad 3,46029,63267,5746. And for this the absolute number 2886 ought to be set aside across the table; here the logarithm found is added to the given logarithm, and the total except the characteristic is 0,99988,69497,8127. This I seek in the 100th Chiliad, where the nearest smaller logarithm I discover to be 4,99988,27246,5701. And across from that 99973, which is increased by the proportional part to 99973,97261,3004. The quotient of this number (divided by the number 2886 set aside before) is 34641,01615,1422.³ [p.22.]

We can increase or decrease the Characteristic most often by choice. Complementary Arithmetic

Factors	composite numbers	Logarithms	Factors	composite numbers	Logarithms
4.4.8.8	1024	3,01029,99566,3981	6.8.9	4320	3,63548,374681492
4.4.7	1120	3,04921,80226,7081	7.7.9.9	4410	3,64443,85894,6784
4.4.8.9	1152	3,06145,24790,8719	7.8.8	4480	3,65127,80139,9814
3.4	1200	3,07918,12460,4762	5.9	4500	3,65321,25137,7534
5.5.7.7	1225	3,08813,60887,0055	8.8.8.9	4608	3,66351,24704,1515
2.7.9	1260	3,10037,05451,1756	2.6.7.7.8	4704	3,67246,73130,6807
4.4.8.8	1280	3,10720,99696,4787	6.8	4800	3,68124,12373,7559
4.4.9.9	1296	3,11260,50015,3457	7.7	4900	3,69019,60800,2851
4.6.7.8	1344	3,12839,92687,1780	5	5000	3,69897,00043,3602
3.5.9	1350	3,13033,37684,9500	7.8.9	5040	3,70243,05364,4552
2.8.9	1440	3,15836,24920,9525	8.8.8	5120	3,70926,99609,7583
3.5	1500	3,17609,12590,5568	8.8.9.9	5184	3,71466,49928,6253
4.6.8.8	1536	3,18639,12156,9549	2.6.7.8.8	5376	3,73045,92600,4576
4.4	1600	3,20411,99826,5592	6.9	5400	3,73239,37598,2297
2.9.9	1620	3,20951,50145,4263	5.5.5.5.9	5625	3,75012,25267,8340
3.8.7	1680	3,22530,92817,2586	7.9.9	5670	3,75358,30588,9291
6.6.6.8	1728	3,23754,37381,4287	8.8.9	5760	3,76042,24834,2321
4.7.8.8	1792	3,25333,80053,2611	8.9.9.9	5832	3,76581,75153,0992
3.6	1800	3,25527,25051,0331	6	6000	3,77815,12503,8364
3.7.9	1890	3,27646,18041,7324	5.5.5.7.7	6125	3,78710,60930,3657
6.6.6.9	1944	3,28869,62605,9026	2.6.8.8.8	6144	3,78845,12070,2345
2	2000	3,30102,99956,6398	7.9	6300	3,79934,05494,5358
6.6.7.8	2016	3,30449,05277,7348	8.8	6400	3,80617,99739,8389
4.8.8.8	2048	3,31132,99523,0379	8.9.9	6480	3,81157,50058,7060
6.6.6	2160	3,33445,37511,5093	9.9.9.9	6561	3,81697,00377,5729
4.7.8	2240	3,35024,80183,3416	2.6.7.8	6720	3,82736,92730,5382
4.8.8.9	2304	3,36248,24747,5117	3.5.5.9	6750	3,82930,37728,3102
6.7.7.8	2352	3,37143,73174,0410	3.6.6.7.9	6804	3,83276,43049,4055
4.6	2400	3,38021,12417,1161	2.6.8.8.9	6912	3,83960,37294,7083
5.7.7	2450	3,38916,60843,6453	7	7000	3,84509,80400,1426
5.7.8.9	2520	3,40140,05407,8154	3.6.7.7.8	7056	3,84855,85721,2376
4.8.8	2560	3,40823,99653,1185	4.4.7.8.8	7168	3,85539,79966,5407
4.8.9.9	2592	3,41363,49971,9855	8.9	7200	3,85733,24964,3127
6.7.8.8	2688	3,42942,92643,8178	3.5.7.7	7350	3,86628,73390,8420
3.9	2700	3,43136,37641,5899	2.6.7.9	7560	3,87852,17955,0121
4.7	2800	3,44715,80313,4222	2.6.8.8	7680	3,88536,12200,3151
4.8.9	2880	3,45939,24877,5923	2.6.8.9.9	7776	3,89075,62519,1822
3	3000	3,47712,12547,1966	4.4.7.7	7840	3,89431,60626,8443
6.8.8.8	3072	3,48742,12113,5948	2.7.7.9.9	7938	3,8997110945,7114
4.8	3200	3,50514,99783,1990	8	8000	3,90308,99869,9914
4.9.9	3240	3,51054,50102,0661	2.7.8.8.9	8064	3,90655,05191,0146
6.7.8	3360	3,52633,92773,8984	9.9	8100	3,90848,50188,7865
6.8.8.9	3456	3,53857,37338,0686	4.4.8.8.8	8192	3,91338,99436,3175
7.7.8.9	3528	3,54752,85764,5978	3.4.7	8400	3,92427,92860,6188
7.8.8.8	3584	3,55436,80009,9009	3.4.8.9	8640	3,93651,37424,7889
4.9	3600	3,55630,25007,6729	2.7.7.9	8820	3,94546,85851,3128
6.7.9	3780	3,57749,17998,3723	4.4.7.8	8960	3,95230,80096,6212
6.8.8	3840	3,58433,12243,6753	9	9000	3,95424,25094,3932
6.8.9.9	3888	3,58972,62562,5424	2.8.8.8.9	9216	3,96454,24660,7914
7.7.9.9	3969	3,59868,10989,0716	3.7.7.8.8	9408	3,97349,73087,3205
4	4000	3,60205,99913,2796	3.5.7.9	9450	3,97543,18085,0926
7.8.8.9	4032	3,60552,05234,3747	2.6.8	9600	3,98227,12330,3957
8.8.8.8	4096	3,61235,99479,6777	2.6.9.9	9720	3,98766,62649,2628
7.6	4200	3,62324,92903,9790	2.7.7	9800	3,99122,60756,9249

[Table 11 - 1.]

[p.23.]

	<i>proportions</i>	<i>Logarithms</i>		
	1-----	0	}	To be given
	.1200 <i>A</i>	1,53959,06230,2381		
	1200 -----	3,07918,12460,4762		
	10	1,00000,00000,0000		
	<i>A</i>	1,53959,06230,2381		
	<i>B</i>	0,46040,93769,7619		Complement
2886	<i>C</i>	3,46029,63267,5746		Nearest to the Complement
Sum of <i>A</i> and <i>C</i>		0,99988,69497,8127		
		42251,2426		Difference
<i>H</i>	99973	0,99988,27246,5701		
		43440,9600		Difference
	99974	0,99988,70687,5301		
	proportions	434409600	}	Given differences
		422512426		
		1---		
		<u>0972613004</u>		
				Proportional part to be added

Product to be divided *H* 99973972613004 Absolute number increased

Factors Divisor 2886
 Quotient 34641016151422

[Table 11 - 2].

All these are demonstrated by Axiom 2, Ch.2. Indeed .1200 is now the other remaining factor: but 2886, with which the logarithms added gives 0,99988,69497,8127 equal to the logarithm of the product, undoubtedly of the number 99973,97261,3004. This product divided by the given factor 2886 gives as the quotient, the remaining factor in question 34641,01615,1422, which is almost equal to the mean proportional sought 34 641016151377546.

But since with division by this method which is, for a number with four places, exceedingly painstaking⁴, I have thought other composite numbers should be selected, which are shown on the preceding page [Table 11-1]. The numbers on the left are factors, from which by continued multiplication, they become those composite numbers; while to the right are the logarithms of the same. For if a number is divided by a composite number, the place of the divisor is taken by the factors of the same, which find the required quotient more easily. But how this ought to be done I show by an example. The mean proportional between 1 and 10800 is sought, the logarithm of this is 4,03342,37554,8695. The logarithm of the mean sought is the half of this, 2,01671,18777,4347, of which the complement is 0,98328,81222,5653. The logarithm found in the table here described

nearest to this is 0,98227,12330,3957 (to which 9600 is situated straight across), which added to that given gives 0,99898,31107,8304, the logarithm of the number 99766, which is corrected by the proportional part: 99766,12651, 6521. This divided by 9600, (or in turn by 2, 6, 8 as I have advised in Lemma 2, Ch. 5) 1039230484547 is the quotient.

You will be able to consider here how this method works:

		<i>Logarithms</i>	
proportions -	{	1----- l. 10800 A 10800 -----	} Given
		0 2,01671,18777,4347 4,03342,37554,8695	
		10 A B 9600 C Sum of A and C	Complement Nearest to the Complement Difference
[p.24.]		1,00000,00000,0000 2,01671,18777,4347 0,98328,81222,5653 0,98227,12330,3957 0,99898,31107,8304 5507,4025	
	H	99766 4,99898,25600,4279 43532,0933	Difference
		99767 4,99898,69131,5212	
	proportions	{ 435310933 55074025 1----- 126516521	} Given differences
	H	99766126516521	Proportional part to be added Absolute number increased
	Factors of the number 96 are 2.6.8, which are divisors of the number H found		
	H	to be divided	99766126516521
	Divisor 8)		124707658145651 First quotient
	Divisor 6)		2 0784609690942 Second quotient
	Divisor 2)		<u>1 0392304845471</u> Final quotient
			103923048454133 The required mean for finding the square root.

This final quotient is a little more than the required mean

[Table 11-3.]

Here finally we consider the characteristic, hitherto almost ignored for the whole working .

Indeed, since the logarithm of the number A shall have 2 for a characteristic, the first three places sought for the root, designate the units of the whole number, while the following places express the numerator of the fraction added on, as indicated before in Ch.4. Between this and the previous working, this is hardly different, because the number nearest the complement was sought previously among the Chiliades; here however it is sought in the table of composite numbers here described: in that place the first divisor can be a prime number; here truly it will always be a composite number, in place of which all the divisors can be substituted, which allow the same

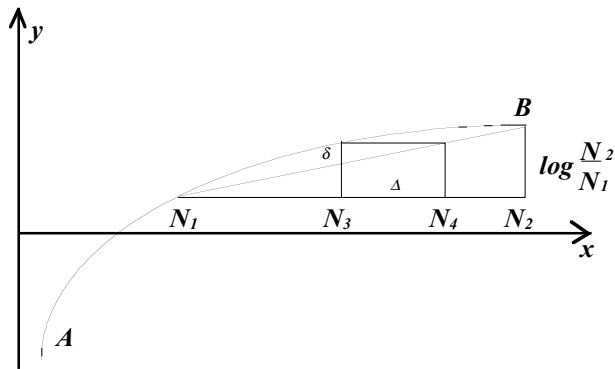
quotient to be found more easily. As for the divisor 9600: 8, 6, & 2 are substituted, of which the first divides the given number, the second the given quotient, the third that second quotient.

§11.3. Notes On Chapter Eleven.

¹ A Chiliad represents a thousand, we get the prefix 'kilo' from it. Briggs is describing the actual tables of logarithms, which form a large and profoundly impressive part of the *Arithmetica*.

² Briggs' 'inconvenience' is shown here using co-ordinates: AB is the log curve drawn

schematically: δ is the deficiency, if the co-ordinate $\log N_3$ is estimated by proportionality for a known N_3 , from similar triangles; while N_4 is the number estimated from



proportionality, too large by Δ , for a known log value at the ordinate N_3 .

Figure 11 - 1.

³ Briggs tries to come to terms numerically with the non-linear nature of the log function in this chapter, in his attempts to evaluate either the logarithm of a number lying between numbers with known logarithms, or the value of a number with a known logarithm similarly placed between known values. Thus, if $N_1 < N_3 < N_2$, the approximate proportionality he considers is:

$$\frac{\log(N_2/N_1)}{N_2 - N_1} \sim \frac{\log(N_3/N_1)}{N_3 - N_1}$$

, with the intention of finding either N_3 or $\log N_3$, one of which is given.

Now, if $N_2 = N_1 + 1$, and $N_3 = N_1 + x$, for $0 < x < 1$, then the approximate proportionality is reduced to $\frac{\log(1+1/N_1)}{1} \sim \frac{\log(1+x/N_1)}{x}$, which is true if the first term only in the Mercator expansion is significant, which is the case for a large enough value of N_1 being chosen, near the end of the log tables.

Now consider the logarithm A in Table 11-2, corresponding to the unknown positive number a , or $\sqrt{1200}$, of which the best estimate is required. We cannot ignore powers of ten in our analysis: hence, the number $a/10$ lies between 1 and 10; the complementary number b (also known only by

its logarithm B) satisfies $ab/10 = 10$. A number c (2886/1000) is selected from the Chiliads which has a logarithm C just less than the complement $\log B$; the product $ac/10^4$ is formed, which from its logarithm is just less than 10. By inspection of the Chiliades, the numbers h (99973) and $h + 1$ (99974) with known logarithms $\log H$ and $\log (H + 1)$ satisfy $\log H < \log (ac) < \log (H + 1)$ and hence $h < ac < h + 1$. The above approximate proportionality is set up: $\frac{\log((h+1)/h)}{1} \sim \frac{\log(ac/h)}{ac-h}$; Figure 11 - 2 shows the appropriate numerical ratios, from which $AE = x < 1$ is found, where $ac = h + x$, and $a = (h + x)/c = 9973.972613004/2886 = 34.641016151422$. (The true value being 34.6410161513775), as Briggs now asserts).

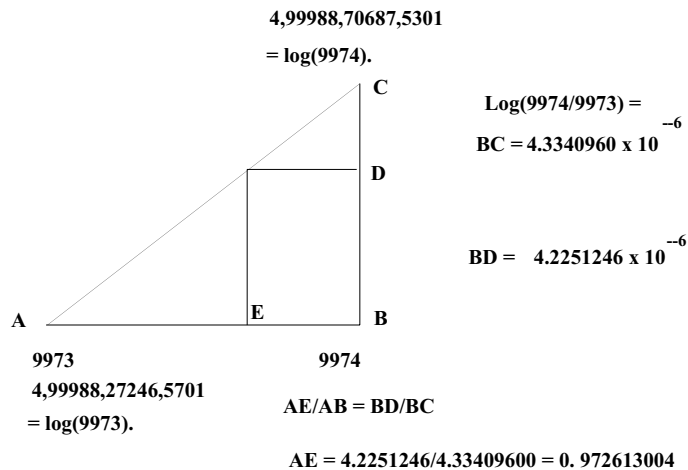


Figure 11 - 2.

⁴ Another example is shown, where a series of divisions by the smaller factors of a composite number is easier to perform than the long division process considered above.

§11.4.

Caput XI. [p.21.]

Numerum in Chiliadibus repertum, per partem proportionalem emendare.

Ostendimus quibus modis omnium numerorum primorum & compositorum, integrorum & partium, Logarithmos invenire poterimus. horum, triginta Chiliades his descriptas habemus, duabus columnis comprehensas. Earum prior versus sinistram, continet numeros absolutos naturali serie crescentes, ab Unitate ad 20000: deinde hac serie interrupta, a 90000 ad 100000. Altera columna priori contigua, habet numerorum absolutorum logarithmos, eorumque differentia. quae non solum ostendunt menda, si quae forte irrepserint, sed etiam partem subministrant proportionalem, quoties usus postulabit; ut aliquid quaerimus accuratius eo, quod in ipso abaco habetur. illa autem pars proportionalis, quae per has acquiritur differentias, non est absolute perfecta; sed semper aliquantulum recedit ab ea quam quaerimus accurata veritate. cum enim numeri absoluti ubique crescant aequaliter, Logarithmi autem quod sunt maiores eo minora habent

incrementa: si pro numero absoluto, Logarithmus numeri proxime, sit per partem proportionalem augendus, pars illa per differentiam interiectam quaesita, erit semper minor quam oportuit. contra autem, si pro Logarithmo dato quaeratur numerus absolutus, is per partem proportionalem auctus erit iusto maior. Idem accidit incommodi in Sinubus, Tangentibus Secantibus; omninoque in omnibus tabulis numerorum, ubi differentiae ex altera parte aequales reliquae inaequales. Veruntamen quo minor est differentiarum inequalitas, eo minor erit aberratio a vero. Ea de causa, pars proportionalis longius recedit a vero in prioribus Chiliadibus, quam in posterioribus, ad quas (quoties opus postulat, & otium fuerit, numerum quaesitum accuratius investigare) provocare poterimus, ad hunc modum.

Datus Logarithmus (cuius numerus absolutus quaeritur) in primis deponat Characteristicam (quae numerum quaesitum nullo modo mutare potest, sed tantum promovere in gradum altiore & ab Unitatem loco remotiore.) deinde auferare e Logarithmo Denarii 1,00000,00000,0000. reliquis non incommode vocari poterit complementum Arithmeticum. hunc reliquum (addita prius Characteristica quae nobis visa fuerit commodissima) quaeramus inter Chiliades. sumaturque Logarithmus proxime minor. & (numero eiusdem absoluto ad tempus seposito) additur dato Logarithmo. totus incidet necessario in ultimam Chiliadem, in qua sumendus est numerus absolutus eidem congruens. quem per partem proportionalem adiectam emendare poterimus. hunc numerum inventum & emendatum, dividat prior numerus antea sepositus; quotus erit numerus dato Logarithmo congruens, quem in primis quaerebamus. huius praecepti hoc cape exemplum. Quaerendus sit medius proportionalis inter Unitatem & 1200 huius Logarithmus est 3,07918,12460,4762. medii autem quaesiti Logarithmus est huius dimidius, ex definitione Logarithmorum, cap.1. & 2.ax.cap.2. nempe 1,53959,06230,2381. qui deposita Characteristica ablatu e 1,00000,00000,0000 relinquit 0,46040,93769,7619. cui proximus, si Characteristicam negligamus, in Chiliade tertia reperitur 3,46029,63267,5746. eique e regione numerus absolutus seponendus 2886; hic Logarithmus repertus addatur dato, totus praeter Characteristicam erit 0,99988,69497,8127. hunc quaero in Chiliade centesima, ubi proxime minorem invenio 4,99988,27246,5701. eique e regione 99973, qui per partem proportionalem auctus sit 99973,97261,3004. huius numeri (divisi per 28860, numerum ante sepositum) quotus erit 34641,01615,1422.

[p.22.]

Factors	numeri comp.	Logarithmi.	Factors	numeri comp.	Logarithmi.
4.4.8.8	1024	3,01029,99566,3981	6.8.9	4320	3,63548,374681492
4.4.7	1120	3,04921,80226,7081	7.7.9..9	4410	3,64443,85894,6784
4.4.8.9	1152	3,06145,24790,8719	7.8.8	4480	3,65127,80139,9814
3.4	1200	3,07918,12460,4762	5.9	4500	3,65321,25137,7534
5.5.7.7	1225	3,08813,60887,0055	8.8.8.9	4608	3,66351,24704,1515
2.7.9	1260	3,10037,05451,1756	2.6.7.7.8	4704	3,67246,73130,6807
4.4.8.8	1280	3,10720,99696,4787	6.8	4800	3,68124,12373,7559
4.4.9.9	1296	3,11260,50015,3457	7.7	4900	3,69019,60800,2851
4.6.7.8	1344	3,12839,92687,1780	5	5000	3,69897,00043,3602
3.5.9	1350	3,13033,37684,9500	7.8.9	5040	3,70243,05364,4552
2.8.9	1440	3,15836,24920,9525	8.8.8	5120	3,70926,99609,7583
3.5	1500	3,17609,12590,5568	8.8.9.9	5184	3,71466,49928,6253
4.6.8.8	1536	3,18639,12156,9549	2.6.7.8.8	5376	3,73045,92600,4576
4.4	1600	3,20411,99826,5592	6.9	5400	3,73239,37598,2297
2.9.9	1620	3,20951,50145,4263	5.5.5.5.9	5625	3,75012,25267,8340
- - - -	- - - -	- - - - - - - -	- - - -	- - - -	- - - - - - - -
7.8.8.9	4032	3,60552,05234,3747	2.6.8	9600	3,98227,12330,3957
8.8.8.8	4096	3,61235,99479,6777	2.6.9.9	9720	3,98766,62649,2628
7.6	4200	3,62324,92903,9790	2.7.7	9800	3,99122,60756,9249

[p.23.]

<i>prop.</i>	{	1-----	<i>Logarithmi.</i>	}	dati	
		.1200 <i>A</i>	0			
		1200 -----	1,53959,06230,2381			
			3,07918,12460,4762			
		10	1,00000,00000,0000			
		<i>A</i>	1,53959,06230,2381			
		<i>B</i>	0,46040,93769,7619		Complementum.	
		2886 <i>C</i>	3,46029,63267,5746		Complemento proximus	
		Summa <i>A, C</i>	0,99988,69497,8127			
			42251,2426		Differentia.	
<i>H</i>		99973	0,99988,27246,5701			
			43440,9600		Differentia	
		99974	0,99988,70687,5301			
		pro-	434409600	}	Differentiae datae	
		port.				422512426
						1---
			0972613004		pars proportionalis addenda	
Factus Dividendus <i>H.</i>		99973972613004			numerus absolutus auctus.	
Factores	Divisor	2886				
	Quotus	34641016151422				

Haec omnia demonstrantur per 2.ax. cap.2. est enim .1200 alter factor, reliquus autem 2886, horum Logarithmi additi sunt 0,99988,69497,8127 aequales Logarithmo facti. nempe numeri 99973,97261,3004 hic factus divisus per datum factorem 2886 dabit in quoto reliquum factorem quaesitum 34641,01615,1422, qui fere aequalis est medio proportionali quaesito 34 641016151377546.

Cum autem huiusmodi divisio, quae sit per numerum quatuor notarum nimis sit operosa, aliquot numeros compositos seligendos putavi, quos praecedens exhibet pagina. numeri a sinistris sunt factores, ex quorum continua multiplicatione fiunt illi compositi. a dextra autem sunt eorundem Logarithmi. Quod si numerus sit a composito dividendus, loco divisoris sumantur factores eiusdem, qui quotum quaesitum facilius invenient. Quomodo autem id fieri debeat exemplo ostendam. Quaeratur medius proportionalis inter 1 & 10800, huius Logarithmus 4,03342,37554,8695. Logarithmus medii quaesiti est huius semissis 2,01671,18777,4347 . huius complementum 0,98328,81222,5653. Logarithmus in abaco hic descripto repertus huic proximus est 0,98227,12330,3957 (cui e regione situs 9600), qui dato additus dat 0,99898,31107,8304. , Logarithmum numeri 99766, qui per partem proportionalem auctus, sit 99766,12651,6521. is divisus per 9600 (vel continue per 2.6.8, ut Lemmata 2, cap. 5 admonui), quotus erit 1039230484547.

Operationis modum hic intueri poteris.

<i>prop.</i>	{	1-----	<i>Logarithmi</i>	}	dati.	
		l. 10800 <i>A</i>	0			
		10800 -----	2,01671,18777,4347			
		10	4,03342,37554,8695			
		<i>A</i>	1,00000,00000,0000			
		<i>B</i>	2,01671,18777,4347		Complementum.	
		9600 <i>C</i>	0,98328,81222,5653		Complemento proximus	
		Sum of <i>A and C</i>	0,98227,12330,3957			
			5507,4025		Differentia.	
<i>H</i>		99766	4,99898,25600,4279			
			43532,0933		Differentia.	
		99767	4,99898,69131,5212			
		pro-	435310933	}	Differentiae datae.	
		port.				55074025
						1-----
			126516521		pars proportionalis addenda.	
<i>H</i>		99766126516521			numerus absolutus auctus.	

Factores numeri 96 sunt 2.6.8, qui sunt divisores numeri *H* inventi.

[p.24.]

<i>H</i> Dividendus	99766126516521	
Divisor 8)	124707658145651	Quotus primus
Divisor 6)	2 0784609690942	Quotus secundus.
Divisor 2)	<u>1 0392304845471</u>	Quotus ultimus.
	103923048454133	medius quaesitus, per inventionem lateris quadrati.

Quotus hic ultimus est medio quaesito paulo maior.

Hic tamen Characteristicam respicimus, huiusque per totam operationem fere neglectam. Cum enim Logarithmus numeri *A*, habeat 2 pro Characteristica, lateris quaesiti tres primae notae, designant integras unitates, subsequentes autem exprimunt numeratorem partium adjiciendarum. ut antea cap.4. Inter hanc & priorem operationem, hic tantum interest. quod numerus complemento proximus, antea quaerebatur inter Chiliadas; hic vero quaeritur in abaco numerorum compositorum hic descripto: illic divisor poterit esse numerus primus; hic vero erit semper compositus, cuius loco alij divisores substitui poterunt, qui eundem quotum facilius invenient. ut pro divisore 9600, substituuntur 8.6.2 quorum primus dividit datum, secundus dati quotum, tertius hunc quotum secundum. substituuntur 8.6.2 quorum primus dividit datum, secundus dati quotum, tertius hunc quotum secundum.